

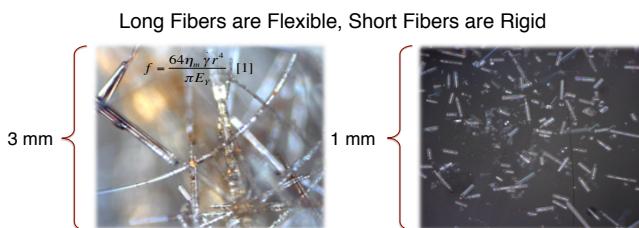
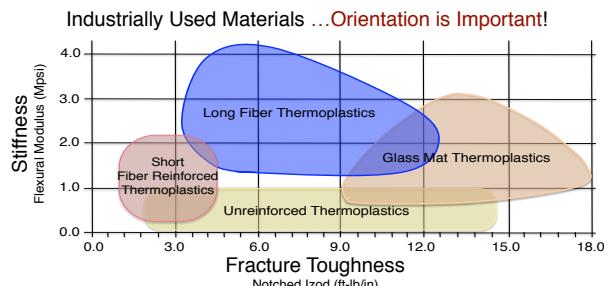
# Transient Shear Rheology of Long Glass Fiber Filled Polypropylene Using a Sliding Plate Rheometer

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## Project Scope:

The manufacturing of Long Glass Fiber Thermoplastic (LGFT) parts possesses competitive advantages in a variety of industries, but the physical characteristics of the final part (shrinkage, warpage, strength, stiffness, etc.) are very dependant on **flow induced fiber orientation**.



## Project Definition:

◇ Use rheology as a tool to provide a link between the deformation response of LGFTs and its transient microstructure, and establish a method for determining unbiased modeling parameters (based on this link).

◇ Evaluate the accuracy of the simulations by comparing numerical predictions with experimentally determined orientations in both simple and complex flows.

## Theory:

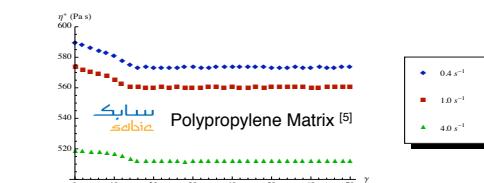
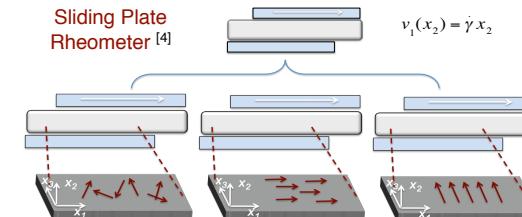
$$\begin{aligned} \underline{\underline{A}} &= \int \vec{p} \vec{p} \psi(\vec{p}, t) d\vec{p} \\ \underline{\underline{A}}_4 &= \int \vec{p} \vec{p} \vec{p} \vec{p} \psi(\vec{p}, t) d\vec{p} \\ \underline{\underline{\kappa}}^T &= \underline{\underline{V}} \underline{\underline{V}} \\ \text{Folgar-Tucker [2]} \quad \frac{D\underline{\underline{A}}}{Dt} &= \underline{\underline{A}} \cdot \underline{\underline{\kappa}}^T + \underline{\underline{\kappa}} \cdot \underline{\underline{A}} - (\underline{\underline{\kappa}} \cdot \underline{\underline{\kappa}})^T : \underline{\underline{A}}_4 + 2C_i \dot{\gamma} (I - 3\underline{\underline{A}}) \end{aligned}$$

Should an orientation model account for fiber flexibility?

Bead-Rod [3]

$$\begin{aligned} \underline{\underline{A}} &= \int \int \vec{p} \vec{p} \psi(\vec{p}, \vec{q}, t) d\vec{p} d\vec{q} \\ \underline{\underline{B}} &= \int \int \vec{p} \vec{q} \psi(\vec{p}, \vec{q}, t) d\vec{p} d\vec{q} \\ \underline{\underline{C}} &= \int \int \vec{p} \psi(\vec{p}, \vec{q}, t) d\vec{p} d\vec{q} \\ \frac{D\underline{\underline{A}}}{Dt} &= \underline{\underline{A}} \left( \underline{\underline{\kappa}}^T + \underline{\underline{\kappa}} \cdot \underline{\underline{A}} - I(\underline{\underline{\kappa}} + \underline{\underline{\kappa}}^T) : \underline{\underline{A}} \right) \underline{\underline{A}} + \frac{l_B}{2} [\underline{\underline{C}} \underline{\underline{\mu}} + \underline{\underline{\mu}} \underline{\underline{C}} - 2(\underline{\underline{p}} \cdot \underline{\underline{C}}) \underline{\underline{A}}] - 2k(l_B - \underline{\underline{A}} \operatorname{tr}(\underline{\underline{B}})) + 2C_i \dot{\gamma} (I - 3\underline{\underline{A}}) \\ \frac{D\underline{\underline{B}}}{Dt} &= \underline{\underline{A}} \left( \underline{\underline{B}} \cdot \underline{\underline{\kappa}}^T + \underline{\underline{\kappa}} \cdot \underline{\underline{B}} - I(\underline{\underline{\kappa}} + \underline{\underline{\kappa}}^T) : \underline{\underline{A}} \right) \underline{\underline{B}} + \frac{l_B}{2} [\underline{\underline{C}} \underline{\underline{\mu}} + \underline{\underline{\mu}} \underline{\underline{C}} - 2(\underline{\underline{p}} \cdot \underline{\underline{C}}) \underline{\underline{B}}] - 2k(\underline{\underline{A}} - \underline{\underline{B}}) \operatorname{tr}(\underline{\underline{B}}) + 2C_i \dot{\gamma} (I + 3\underline{\underline{B}}) \\ \frac{D\underline{\underline{C}}}{Dt} &= \underline{\underline{\kappa}} \cdot \underline{\underline{C}} - (\underline{\underline{A}} : \underline{\underline{\kappa}}) \underline{\underline{C}} + \frac{l_B}{2} [\underline{\underline{\mu}} - \underline{\underline{C}} (\underline{\underline{\mu}} \cdot \underline{\underline{C}})] - k \underline{\underline{C}} [1 - \operatorname{tr}(\underline{\underline{B}})] \\ \underline{\underline{\mu}} &= \sum_{i=1}^3 \left[ \sum_{j=1}^3 \sum_{k=1}^3 \left[ \frac{\partial^2 V_{ij}}{\partial x_k \partial x_k} + K_{ijk} \right] A_{jk} \right] e_i \end{aligned}$$

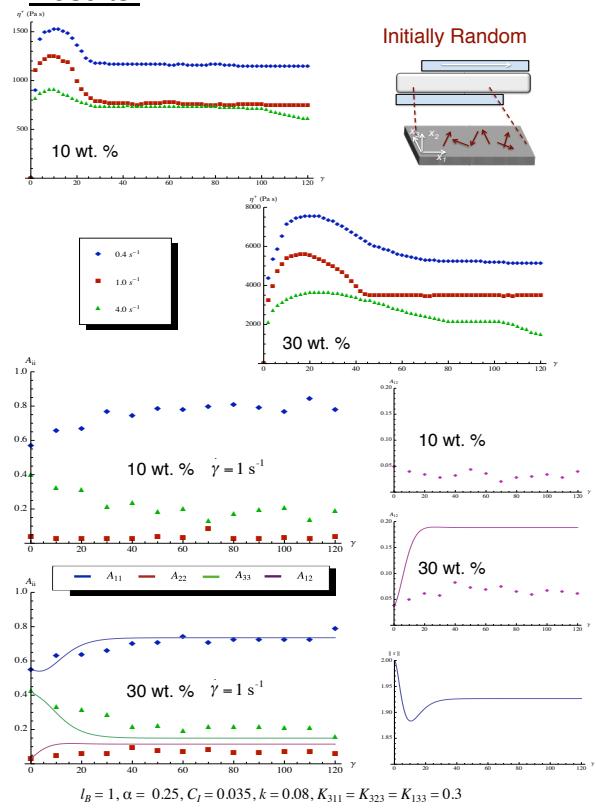
## Experiment:



## References:

- [1] Switzer and Klingenberg, Int. J. Multiphase Fluids, 2002
- [2] Folgar and Tucker, J. Rein. Plast. Comp., 1984
- [3] Strautins and Latz, Rheol. Acta., 2007
- [4] Giacomin McGill University, 1987
- [5] Donated material from Ann Marie Burnell and Sabic

## Results:



## Conclusions:

- ◇ The rheology of LGF filled polypropylene exhibits large transient stress overshoots.
- ◇ Shear thinning occurs with increased shear rate. Also, viscosity is enhanced with increased concentration.
- ◇ Orientation evolution occurs over the same strain region as does the dynamic shear stress response.
- ◇ The Bead-Rod model may be used to approximate the transient orientation, but its link to the rheology is not yet understood.